

Gravity, Projectiles, and Satellites

Physics

In this lesson, we will discuss the following:

Newton's Law of Universal Gravitation

Weight and Apparent Weight

Projectile Motion

Satellite Motion

[Click HERE to watch Neil deGrasse Tyson discuss gravity.](#)

A large, realistic-looking red apple with a brown stem is positioned in the center of the frame, resting on a light-colored, textured stone surface. In the background, a black metal railing is visible, and the ground beyond it appears to be grass. The scene is brightly lit, suggesting an outdoor setting.

Newton's Law of Universal Gravitation


Isaac Newton did not discover gravity, but he discovered that gravity is universal. In other words, Newton found that gravity affects all objects with mass.

Newton's Law of Universal Gravitation

Newton's Law of Universal Gravitation says that all objects with mass are attracted to all other objects with mass.

[Click HERE to watch Bill Nye demonstrate the force due to gravity.](#)

Mathematical Statement of Newton's Law of Universal Gravitation

A large, ripe red apple with a short stem is positioned on a dark metal stand. The apple is the central focus of the image, with its vibrant red color contrasting against the grey metal and the light-colored, textured ground. The background is slightly blurred, showing more of the stand and the ground.

Using experimentation, Newton was able to develop a mathematical statement of his Law of Universal Gravitation.

Mathematical Statement of Newton's Law of Universal Gravitation

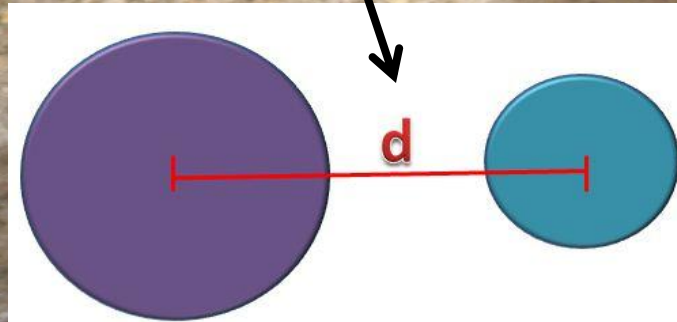
$$F_g = G \frac{m_1 \times m_2}{d^2}$$

The gravitational force between Object 1 and Object 2

The Gravitational Constant: $6.67 \times 10^{-11} \text{ N} \cdot \text{m}^2 / \text{kg}^2$

Masses of Object 1 and Object 2

The distance between the CENTERS of Object 1 and Object 2



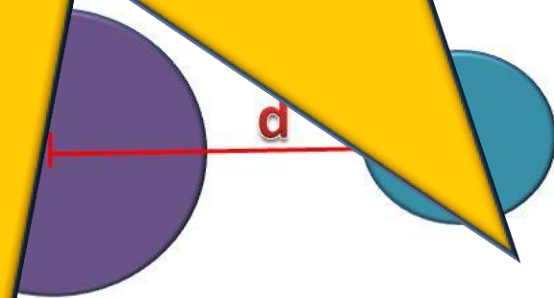
Mathematical Statement of Newton's Law of Universal Gravitation

**The force due to gravity is
always ATTRACTIVE. In other
words, the direction of the
gravitational force on Object 1
is toward Object 2 and vice
versa.**

The gravitational force
between Object 1 and
Object 2

The Gravitational
Constant

1
2



Mathematical Statement of Newton's Law of Universal Gravitation

- In Newton's Law of Universal Gravitation, ***G*** is just a constant, called the Gravitational Constant.

$$G = 6.67 \times 10^{-11} N * m^2 / kg^2$$

- Notice, ***G*** is a tiny number.
- Isaac Newton first came up with ***G*** using experimentation.

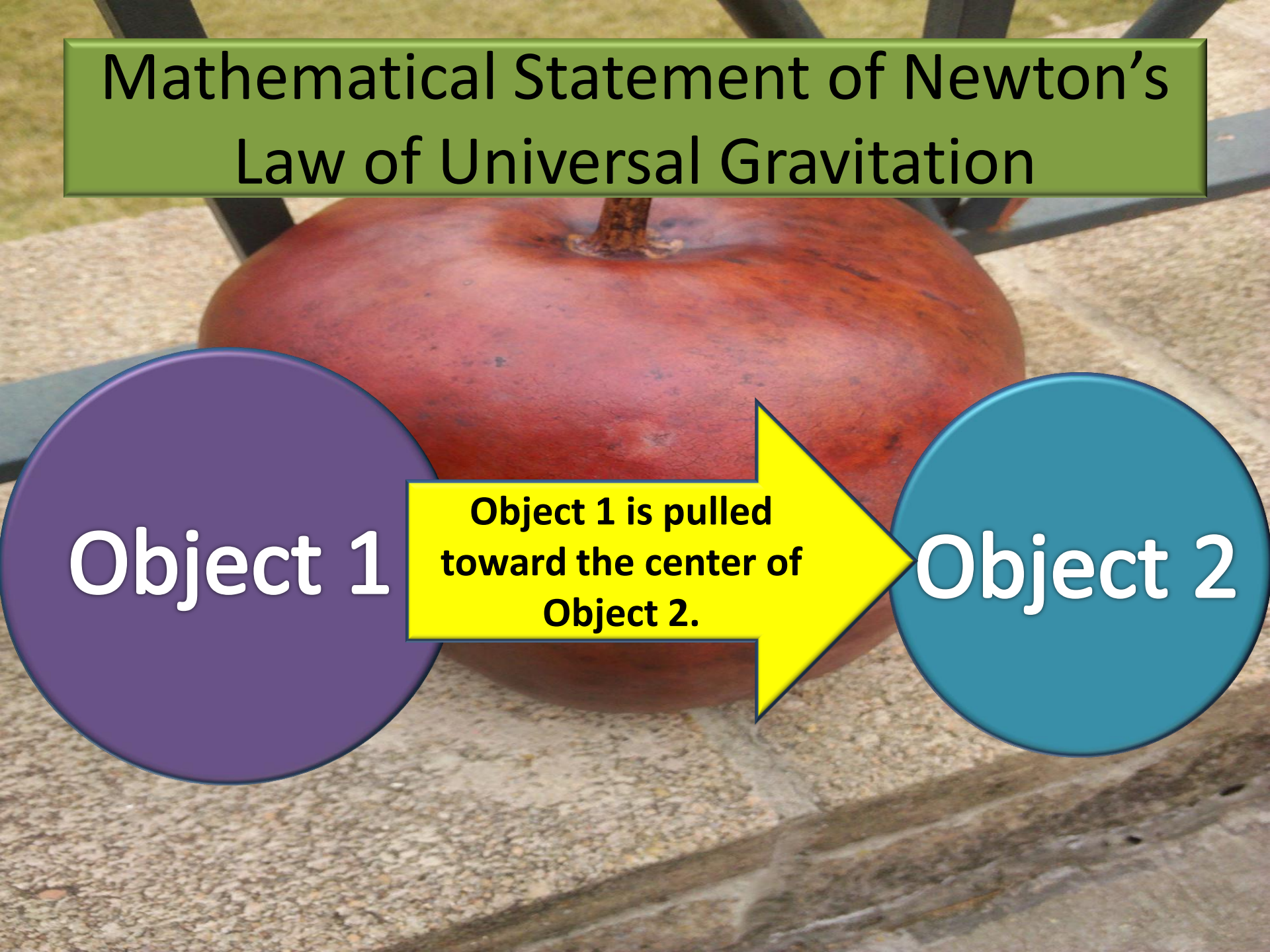
[Click HERE to read an article with some relatively new information about *G*.](#)

Mathematical Statement of Newton's Law of Universal Gravitation

Object 1

**Object 1 is pulled
toward the center of
Object 2.**

Object 2



Mathematical Statement of Newton's Law of Universal Gravitation

Object 1

**Object 2 is pulled
toward the center of
Object 1.**

Object 2

Mathematical Statement of Newton's Law of Universal Gravitation

Object 1

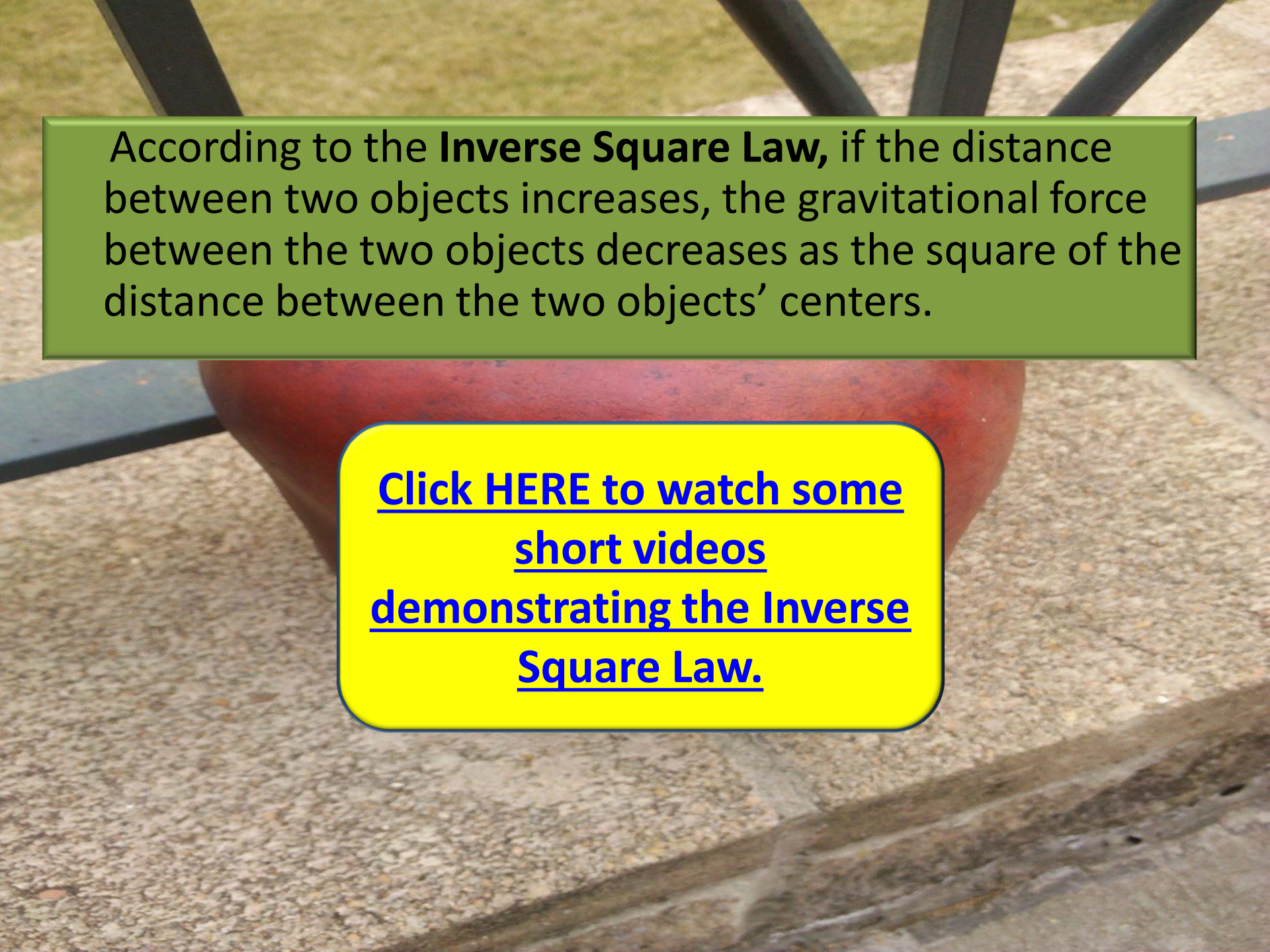
**And, they pull on each other
equally hard, regardless of
how large each object is!**

Object 2

The Inverse Square Law

Newton's
Law of
Universal
Gravitation
follows the
Inverse
Square Law.

[Click HERE to watch a
great demonstration of
the Inverse Square Law.](#)



According to the **Inverse Square Law**, if the distance between two objects increases, the gravitational force between the two objects decreases as the square of the distance between the two objects' centers.

[Click HERE to watch some short videos demonstrating the Inverse Square Law.](#)

How Changing Mass Affects Gravitational Force

- According to Newton's Law of Universal Gravitation, if you increase the sizes of the two objects, the gravitational force between the two increases, also.
- If you decrease the masses of the two objects, the gravitational force between them decreases.

Let's See What You Know

If the distance between two objects is tripled, what happens to the gravitational force between those two objects? Go to the next page to see the correct answer.

The gravitational force is tripled.

The gravitational force is decreased to $\frac{1}{3}$ what it was when the objects were closer.

The gravitational force is increased to 9 times what it was when the objects were closer.

The gravitational force is decreased to $\frac{1}{9}$ what it was when the objects were closer.

Let's See What You Know

$$\vec{F}_g = G \frac{m_1 \times m_2}{d^2}$$

If you triple d , the gravitational force will decrease by a factor of 9 (or 3^2).

was when the objects were closer.

when the objects were closer.

Let's See What You Know

If the **distance** between two objects is halved, what happens to the gravitational force between those two objects? Go to the next page to see the correct answer.

The gravitational force is halved.

The gravitational force is doubled.

The gravitational force is decreased to $\frac{1}{4}$ of what it was when the objects were farther apart.

The gravitational force is quadrupled.

Let's See What You Know

If the **distance** between two objects is

$$\vec{F}_g = G \frac{m_1 \times m_2}{d^2}$$

If you halve d , the gravitational force will increase by a factor of 4 (or 2^2).

farther apart.

Definition of Weight

- When we learned about various forces, we learned that the weight of an object is defined as the gravitational force acting on that object.
- In addition, we learned that the formula for weight is just

$$\vec{F}_g = mg \downarrow$$

Definition of Weight

Same Thing!

$$\vec{F}_g = mg \downarrow$$

$$F_g = G \frac{m_1 \times m_2}{d^2}$$

**This is the same thing as
WEIGHT!**

Definition of Weight

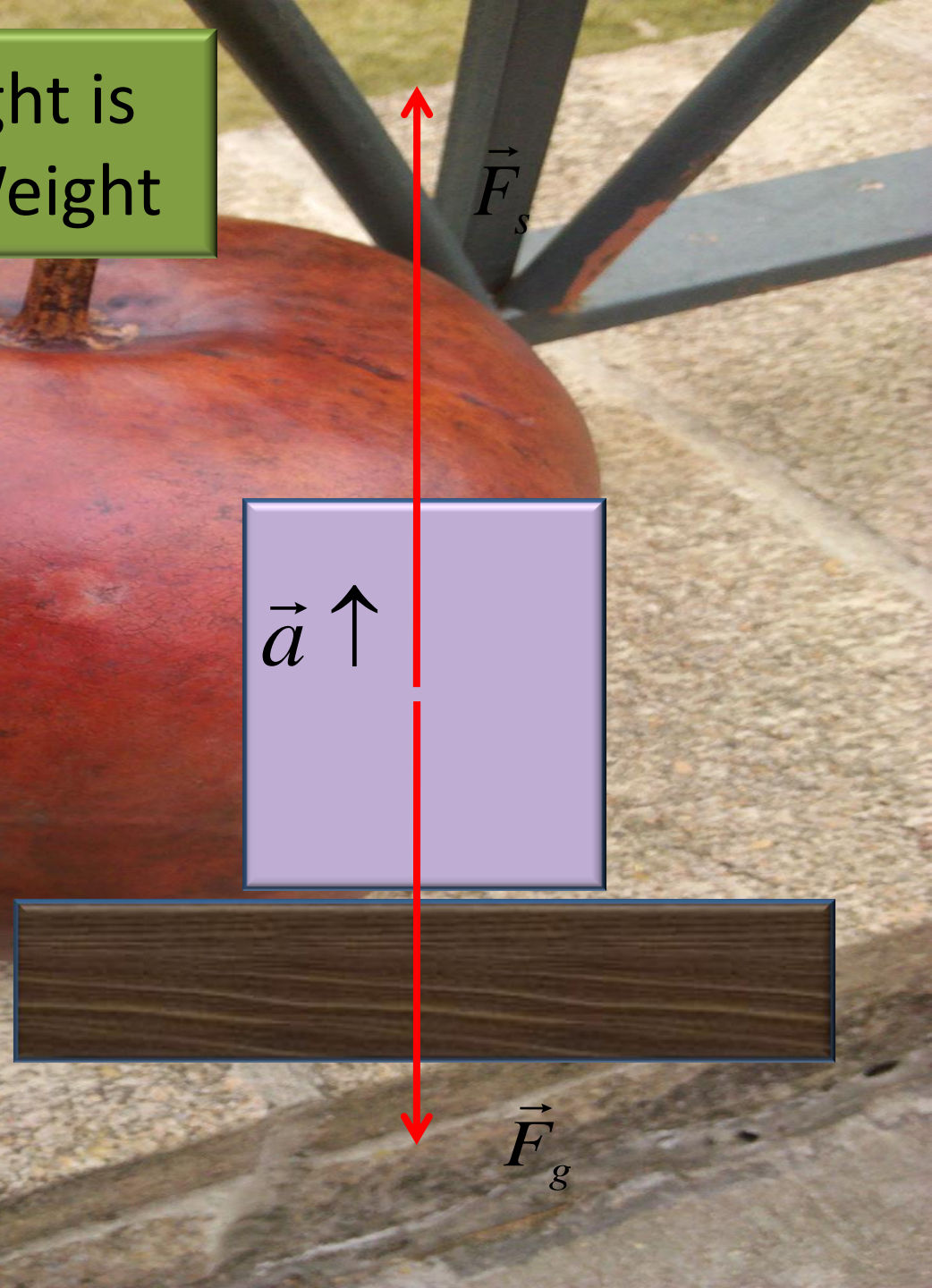
[Click HERE to find out what you would weigh on different planets.](#)

Definition of Apparent Weight

- The **apparent weight** of an object is not exactly the force due to gravity acting on that object, but it is the **SUPPORT FORCE** acting on that object.
- Remember: for an object at rest on a horizontal surface, support force and the force due to gravity are equal in magnitude.
- In other words, if an object is at rest on a horizontal surface, its apparent weight and its actual weight are essentially the same.

When Apparent Weight is Greater than Actual Weight

- When support force is greater in magnitude than the force due to gravity, then apparent weight is greater than actual weight.
- This happens when an object is **ACCELERATING** upward.



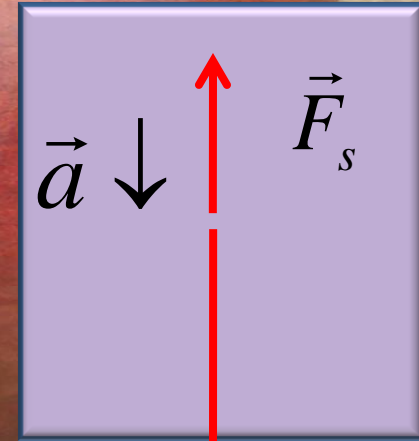
A large, realistic-looking red apple is the central focus of the image. It is resting on a dark metal stand that has several legs. The background is a light-colored, textured surface, possibly concrete or gravel. The apple has a natural, slightly mottled red color with some green at the stem. The text boxes are overlaid on the image: one at the top left and a larger one at the bottom right.

When Apparent Weight is Greater than Actual Weight

- Example: Apparent weight is greater than actual weight in an elevator which is **ACCELERATING** upward.

When Apparent Weight is Less than Actual Weight

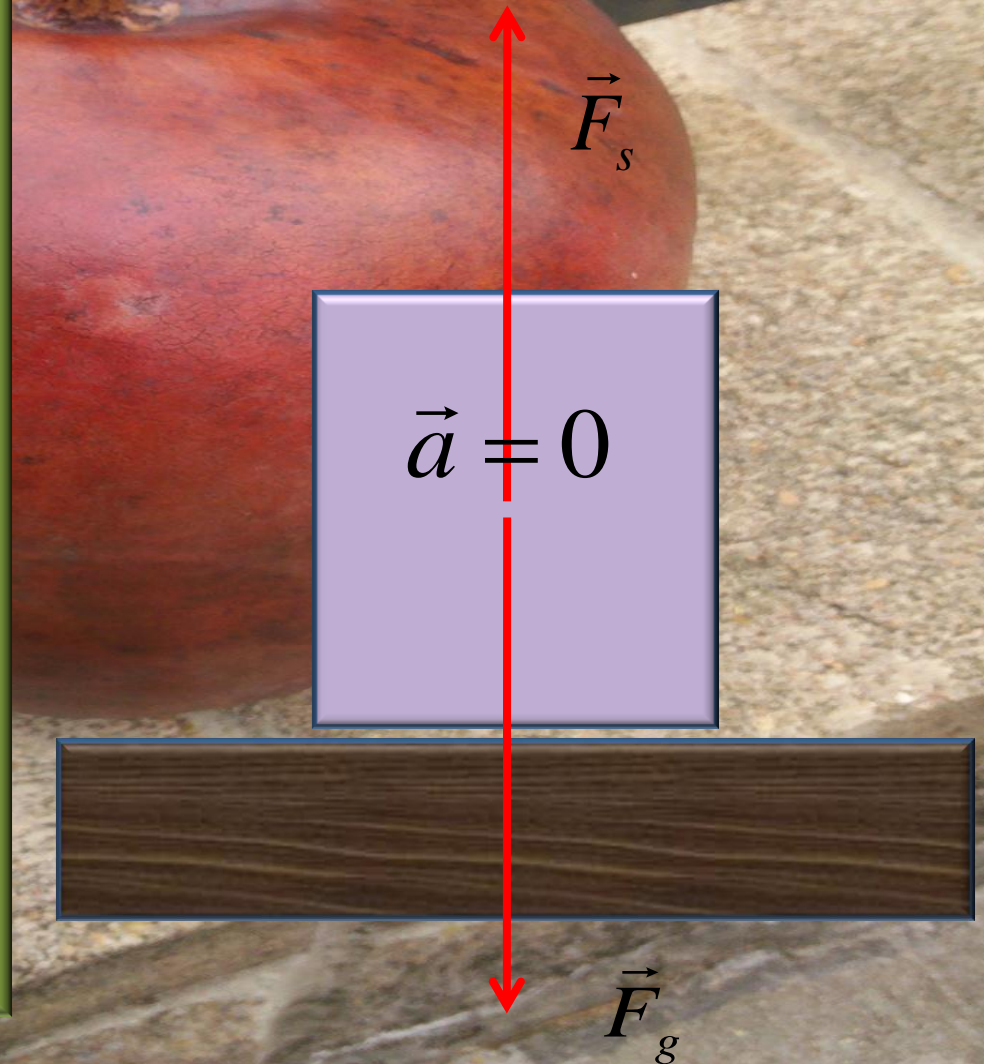
- When support force is smaller in magnitude than the force due to gravity, then apparent weight is less than actual weight.
- This happens when an object is **ACCELERATING** downward.




\vec{F}_g

- When support force is equal in magnitude to the force due to gravity, then apparent weight is the same as actual weight.
- This happens when an object is neither ACCELERATING upward nor ACCELERATING downward.
- This does NOT mean that the object is not MOVING up or down; the object is just not ACCELERATING up or down.

When Apparent Weight
is the Same as Actual
Weight



A large, ripe red apple is shown resting on a light-colored, textured concrete surface. The apple is positioned in the center-right of the frame. In the background, there are dark, vertical metal bars, possibly part of a fence or a playground structure. The overall scene is outdoors with natural lighting.

When there is
no support
force acting on
an object, that
object is
WEIGHTLESS.

Weightlessness

[Click HERE to
find out why
astronauts in
the space
station are
weightless.](#)

- When there is no support force acting on an object, that object is **WEIGHTLESS**.
- In other words, an object feels weightless when it is in **FREE FALL**.

Weightlessness

[Click HERE to see
a great
demonstration.](#)



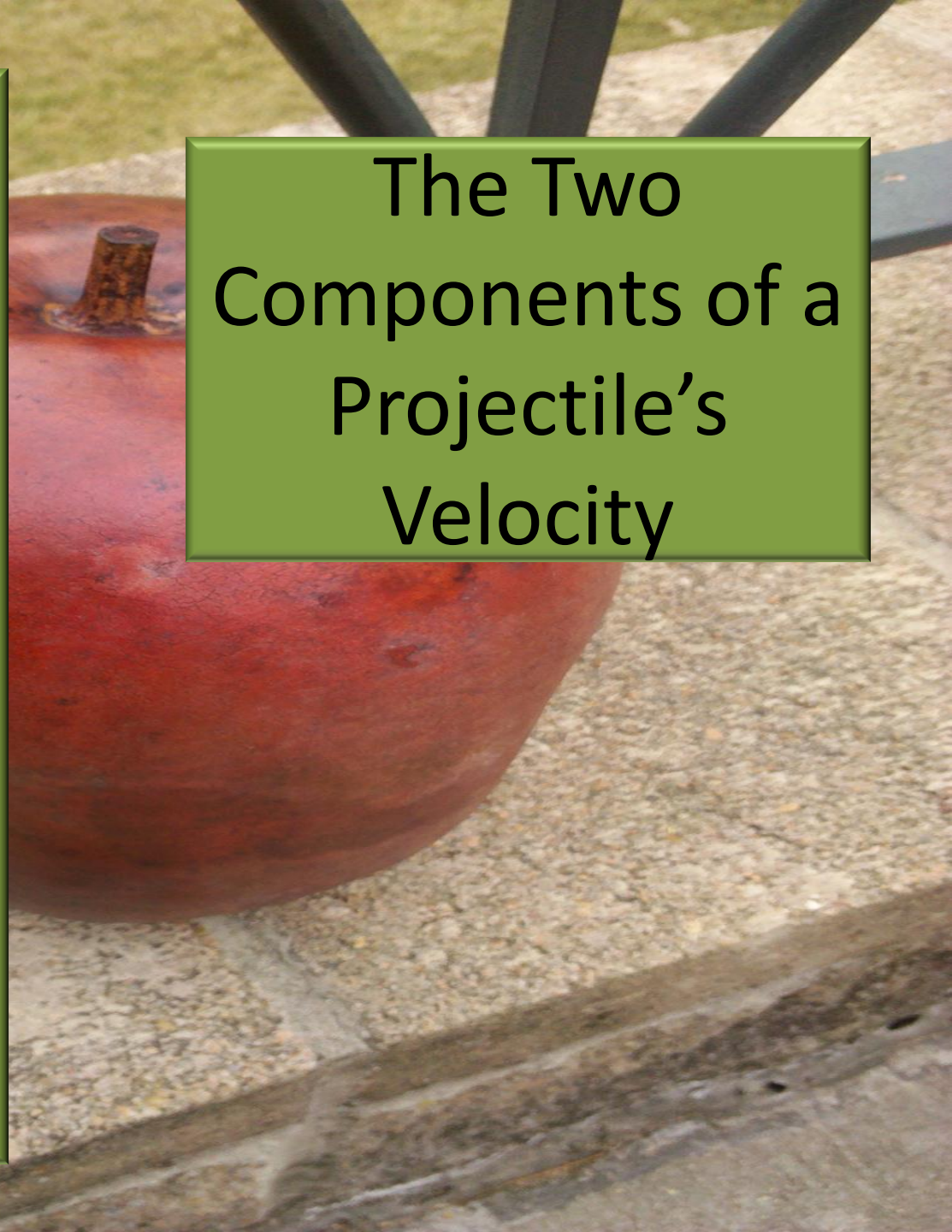
Projectile Motion

- When an object is moving under the influence of gravity, it is called a **PROJECTILE**.
- The motion of a projectile is called **PROJECTILE MOTION**.

[Click HERE to
open a
projectile
motion
simulation.](#)

- When a projectile moves in two dimensions, its motion has two components:
 - A vertical component and
 - A horizontal component.
- Each component is independent of the other component.

The Two Components of a Projectile's Velocity



- The vertical component of a projectile's velocity is affected by the force due to gravity.
- The force due to gravity on a projectile causes the vertical component of the projectile's velocity to have an acceleration of g .

The Vertical Component of a Projectiles' Velocity



[Click HERE to
open another
projectile
motion
simulation.](#)

The Horizontal Component of a Projectiles' Velocity

- For an object in free fall (no wind resistance), the horizontal component of velocity does not have an acceleration because there is no force acting on a projectile in the HORIZONTAL direction.
- In other words, the horizontal component of a projectile's velocity DOES NOT CHANGE when wind resistance is neglected.

Satellite Motion

- A satellite is a projectile that falls around the earth.
- We say that a satellite has just enough ***tangential*** velocity that it does not ever hit the earth's surface when it falls.

If you can figure out what is physically wrong in the video below, post it in the discussion board.



Satellite Motion

- If an satellite stays the same distance from the center of its motion, it is said to be undergoing **uniform circular motion**.
- An object in uniform circular motion moves at a constant speed.
- However, an object undergoing uniform circular motion **is accelerating** because it is constantly changing direction.



Satellite Motion

In order for an object to become an Earth satellite when it is at or near the surface of the earth, it must be traveling with a tangential velocity of about 8 km/s.

- If we set up our system so that no external work is done on or by the system, then the total energy of the system is conserved.
- If we include the earth and a satellite in the system, we can say that the energy of the earth/satellite system is conserved.

Energy is Conserved
for Satellite Motion



Energy is Conserved for Satellite Motion

- If the energy of the earth/satellite system is conserved, then the sum of the kinetic and gravitational potential energies must stay the same, regardless of where the satellite is located in its orbit.
- If the satellite has a smaller gravitational potential energy (if it is closer to the earth), it must have a larger kinetic energy (it must be moving faster).



Escape Speed

- If an object is moving fast enough, it will escape from orbit.
- When an object has reached escape speed, it has escaped orbit, but it will never escape gravity.
- The force due to gravity extends infinitely far away from the source.

From the surface of the earth, escape speed is about 11.2 km/s.